

Image scanning microscopy with quantum and classical correlations

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$$\langle \psi | a^\dagger a a a | \psi \rangle$$

↳ $\delta X = \frac{\lambda}{2 \cdot NA}$

Abbe's limit



Weizmann Institute

Dan Oron

Yaron Silberberg

Bat-el Raphael

Uri Rossman

Yonatan Israel

Gur Lubin



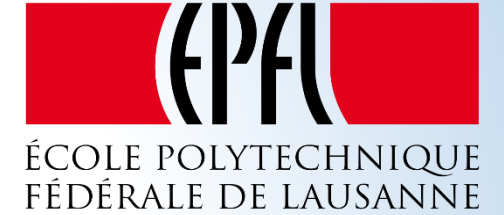
EPFL, AQUA lab

Edoardo Charbon

Claudio Bruschini

Michel Antolovic

Samuel Burri



University of Warsaw

Radek Łapkiewicz

Alexander Krupiński-Ptaszek

Aleksandra Sorda

Adrian Makowski



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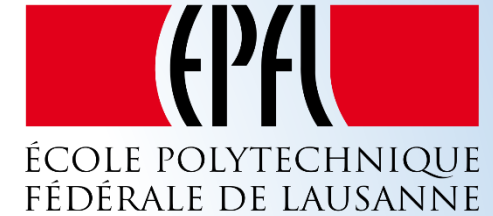
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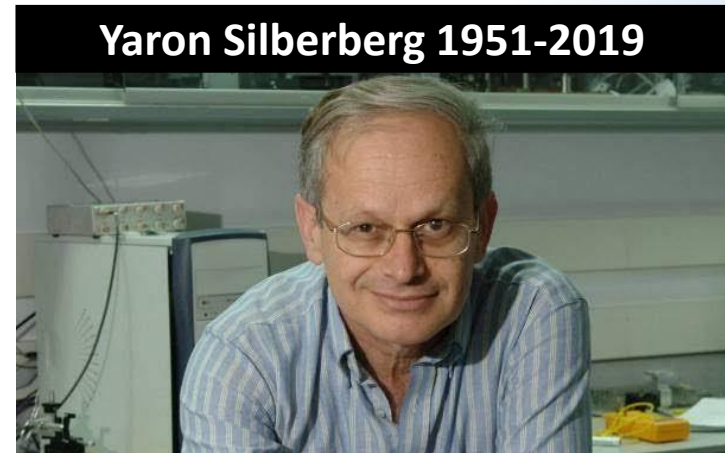
Alexander Krupiński-Ptaszek

Aleksandra Sorda

Adrian Makowski

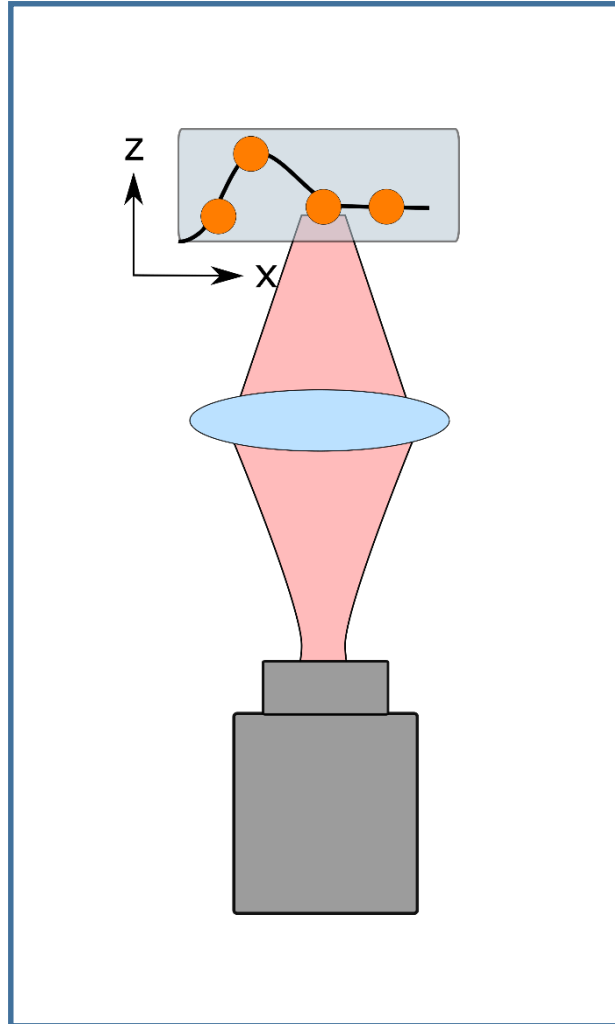


Yaron Silberberg 1951-2019



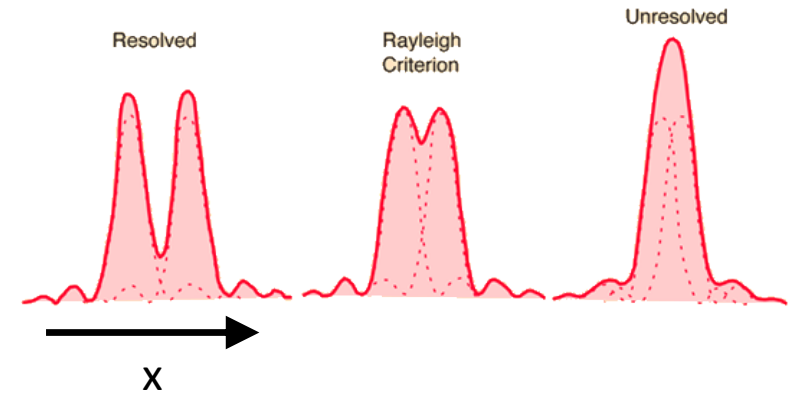


The resolution problem



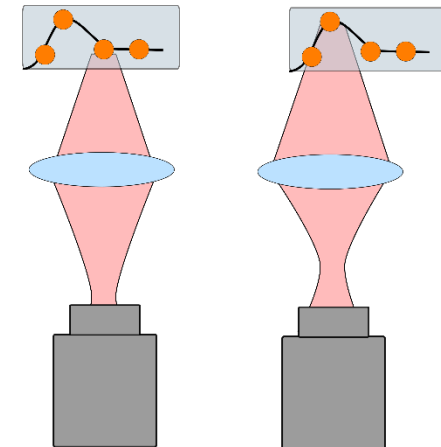
Lateral resolution
Rayleigh criterion

$$\Delta x = 1.22 \cdot \frac{\lambda}{2NA} \sim 200 \text{ nm}$$

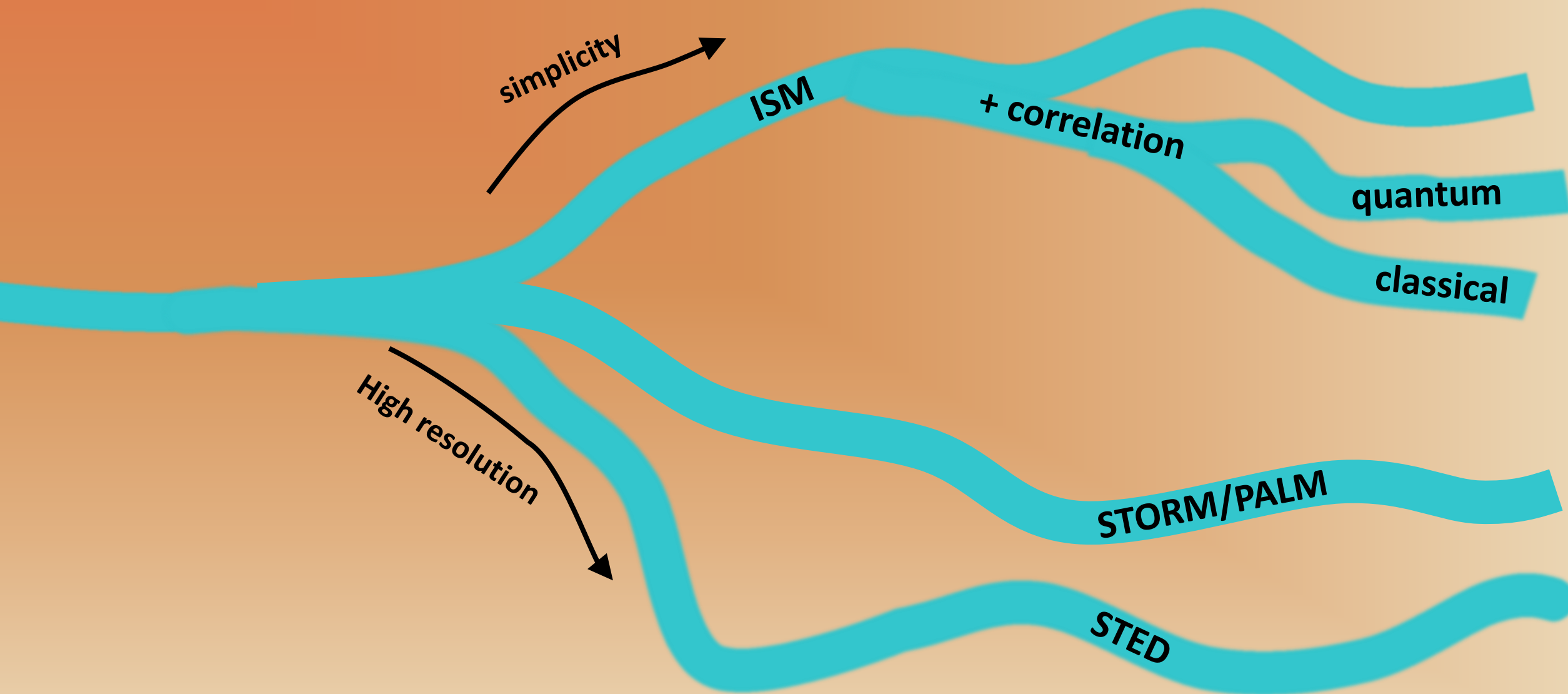


Axial sectioning
Rayleigh range

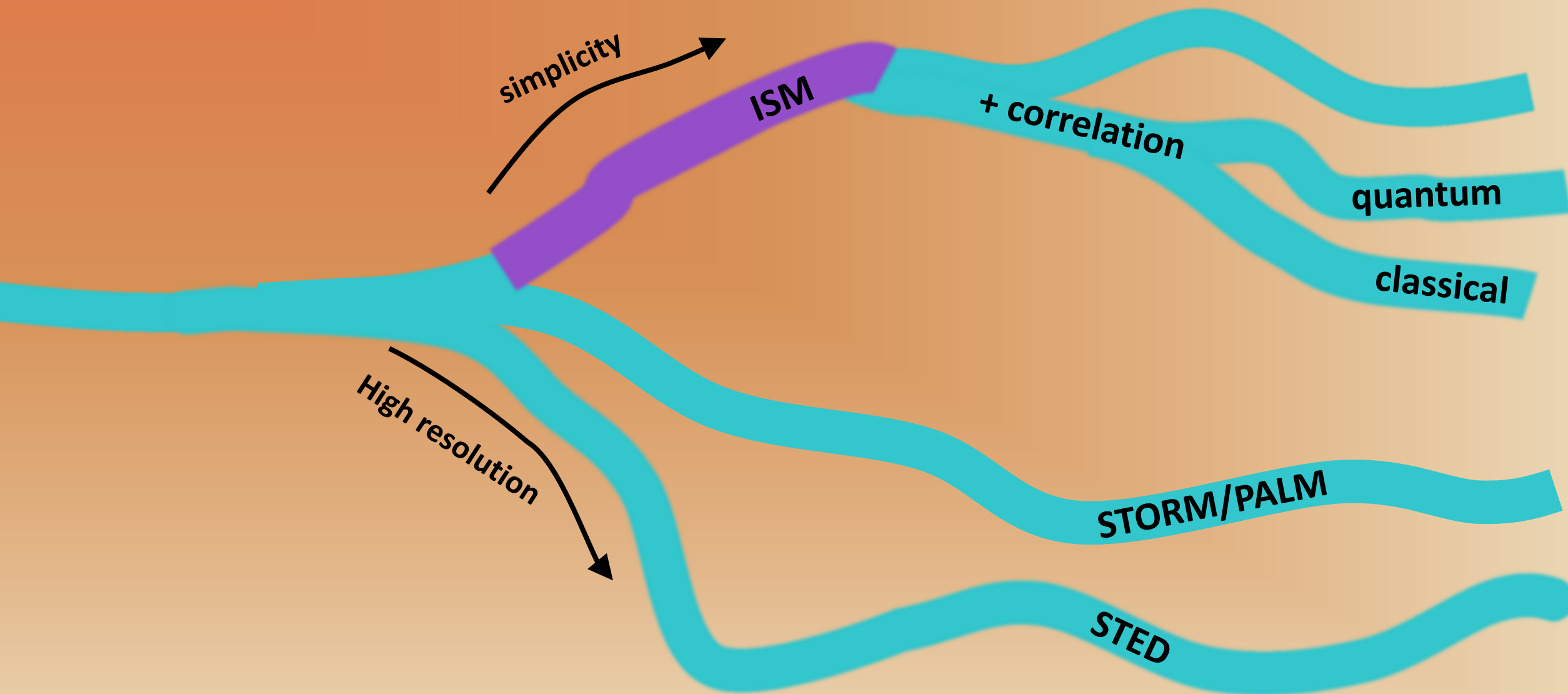
$$\Delta z \sim \frac{\lambda}{(NA)^2} \sim 1 \mu m$$



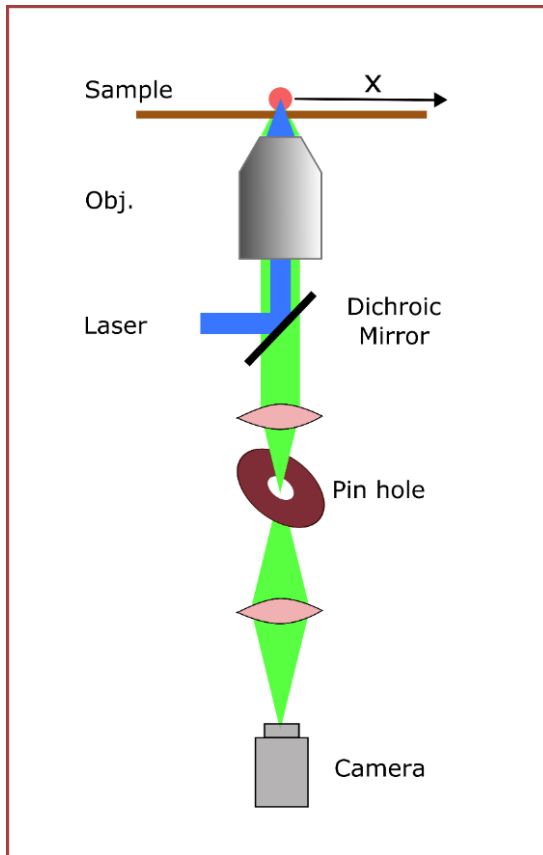
Super-resolution "flow chart"



Super-resolution "flow chart"



Super-resolution in a confocal microscope?

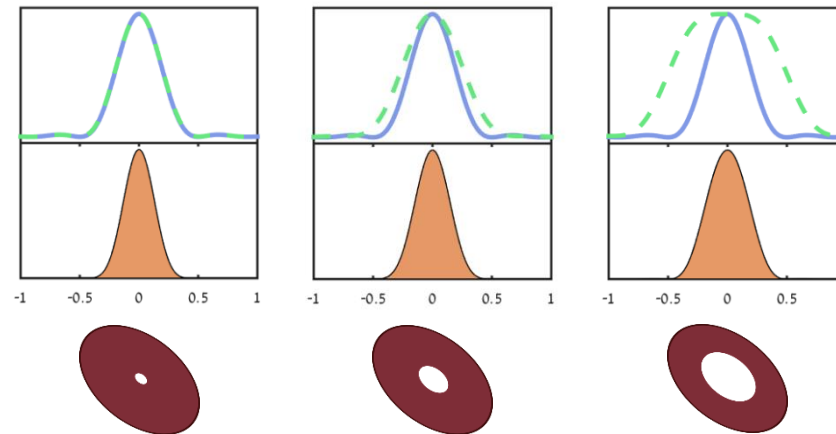


$$P_{\text{signal}} = P_{\text{excitation}} \cdot P_{\text{detection}}$$

0.1 AU

0.5 AU

1 AU



x2 resolution (--)
for the price of
x10 less signal (-)

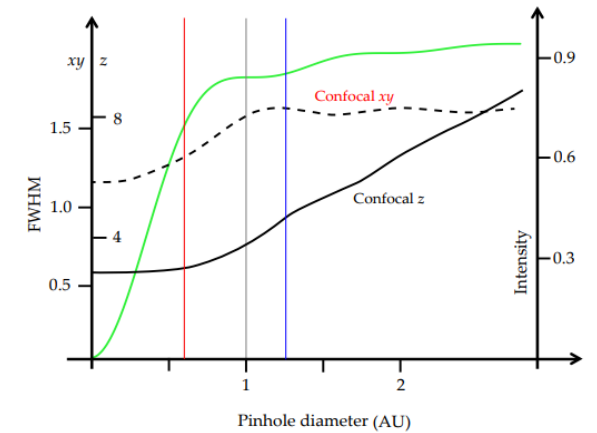
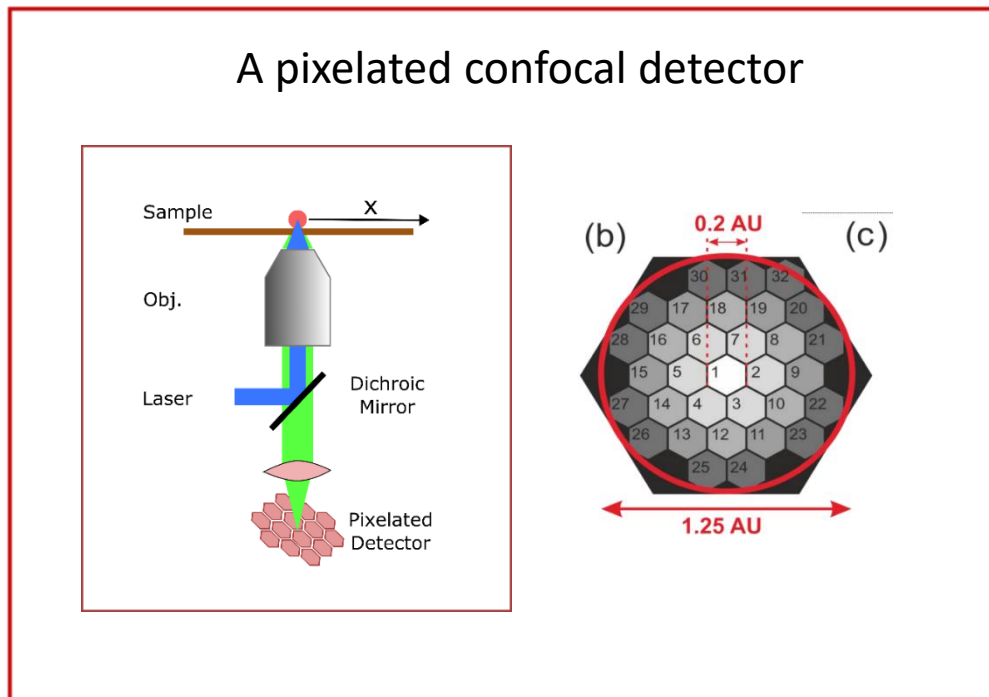
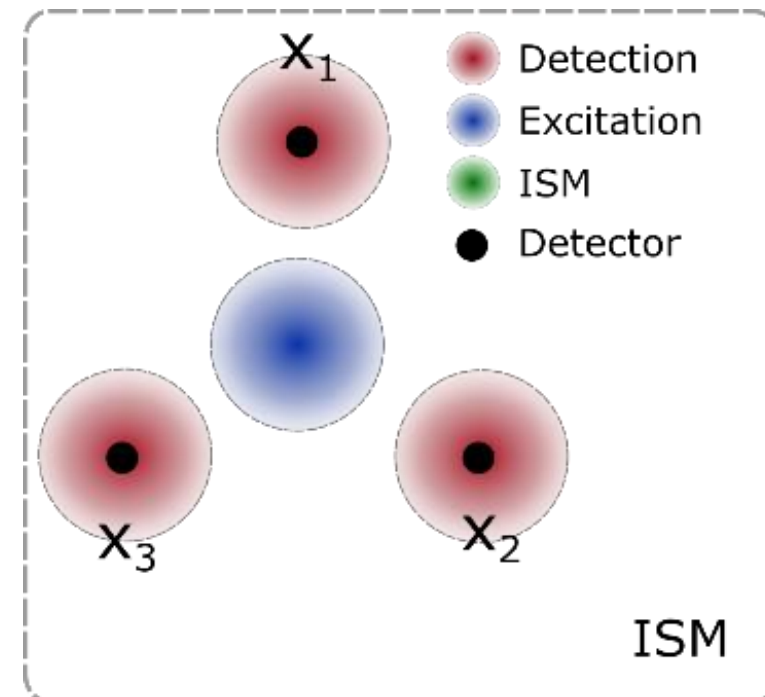


Image Scanning Microscopy \ Airy scan

- Exchange pinhole with a detector array
- Scan sample
- Shift images and sum



$$P_{signal} = P_{excitation} \cdot P_{detection}$$

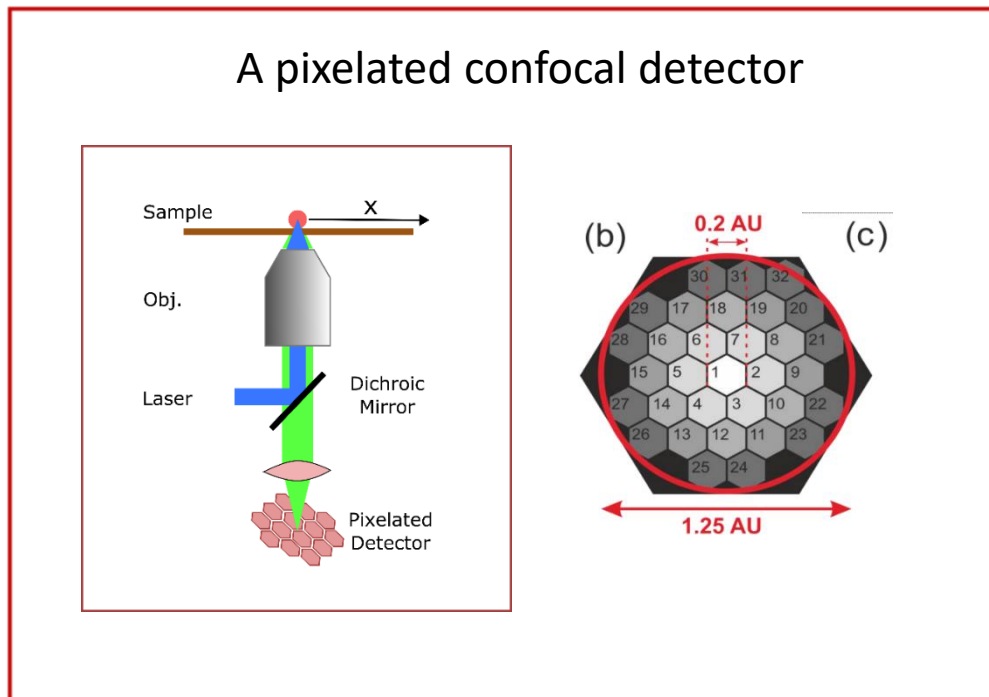


Sheppard, C. J. R. *Optik (Stuttg)*. **80**, 53–54 (1988)

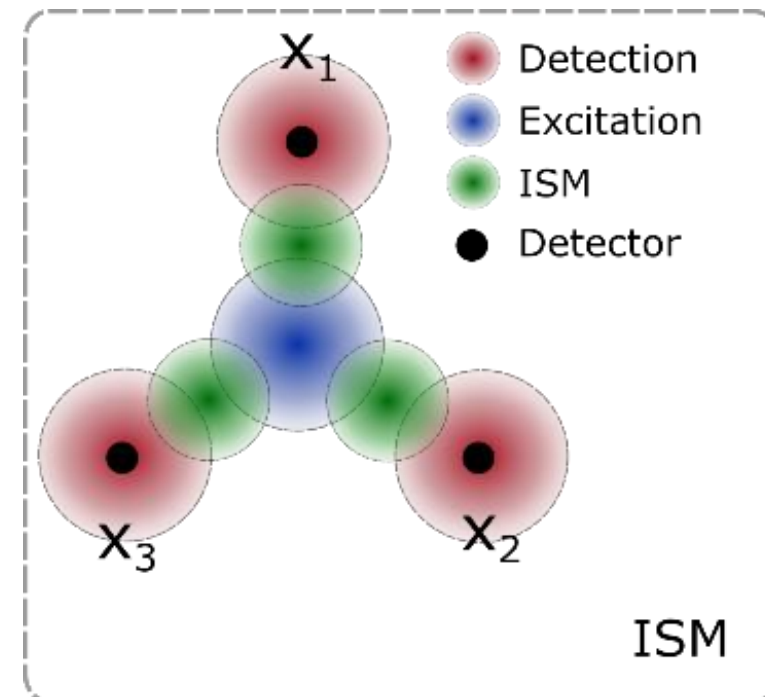
Muller and Enderline, *PRL*, 2010

Image Scanning Microscopy \ Airy scan

- Exchange pinhole with a detector array
- Scan sample
- Shift images and sum



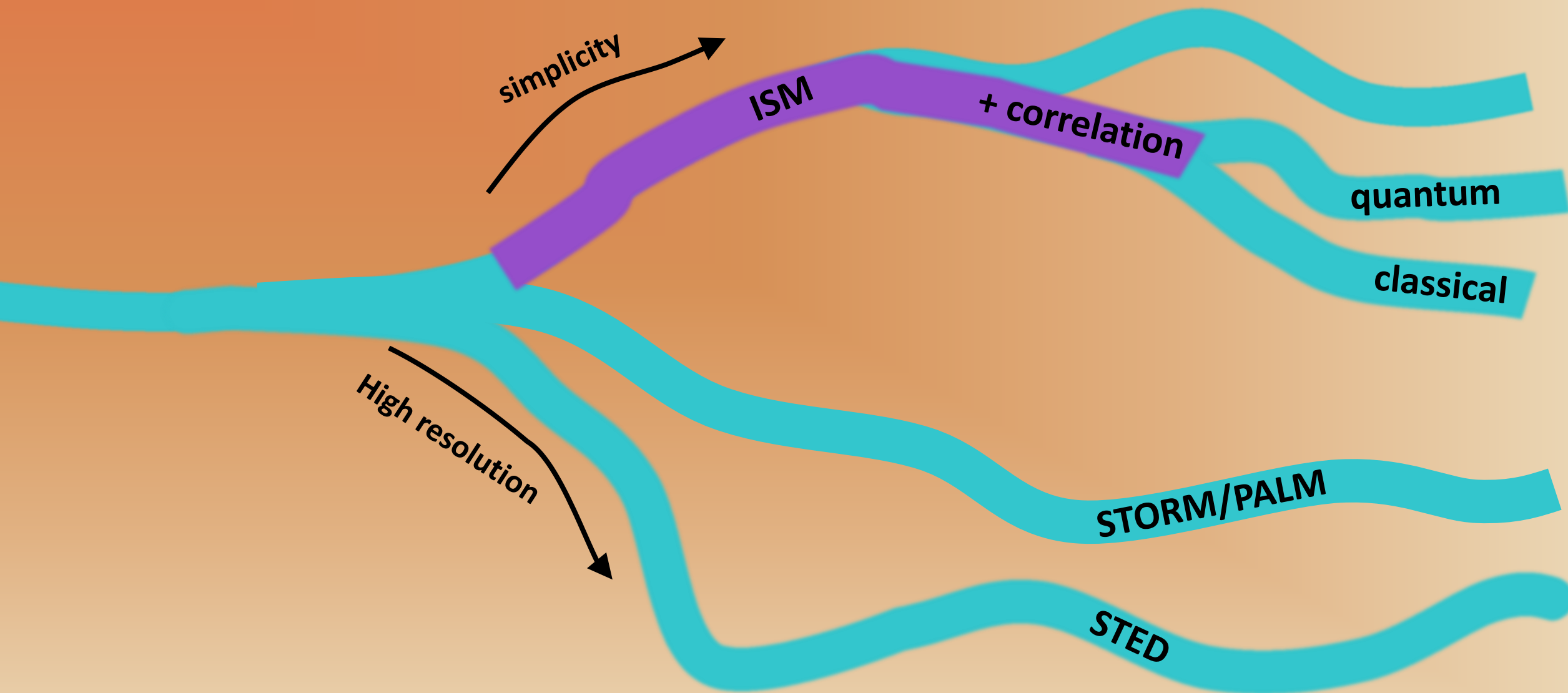
$$P_{signal} = P_{excitation} \cdot P_{detection}$$



Sheppard, C. J. R. *Optik (Stuttg)*. **80**, 53–54 (1988)

Muller and Enderline, *PRL*, 2010

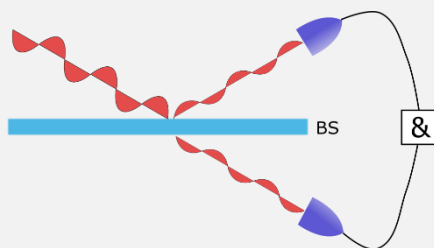
Super-resolution "flow chart"





Temporal correlation: bunching and antibunching

Hanbury-Brown and Twiss setup



$$g^{(2)}(\tau) = \frac{\langle I(t)I(t + \tau) \rangle}{\langle I(t) \rangle^2}$$

Bunching

Intensity fluctuations



$$g^{(2)}(\tau) > 1$$

Antibunching

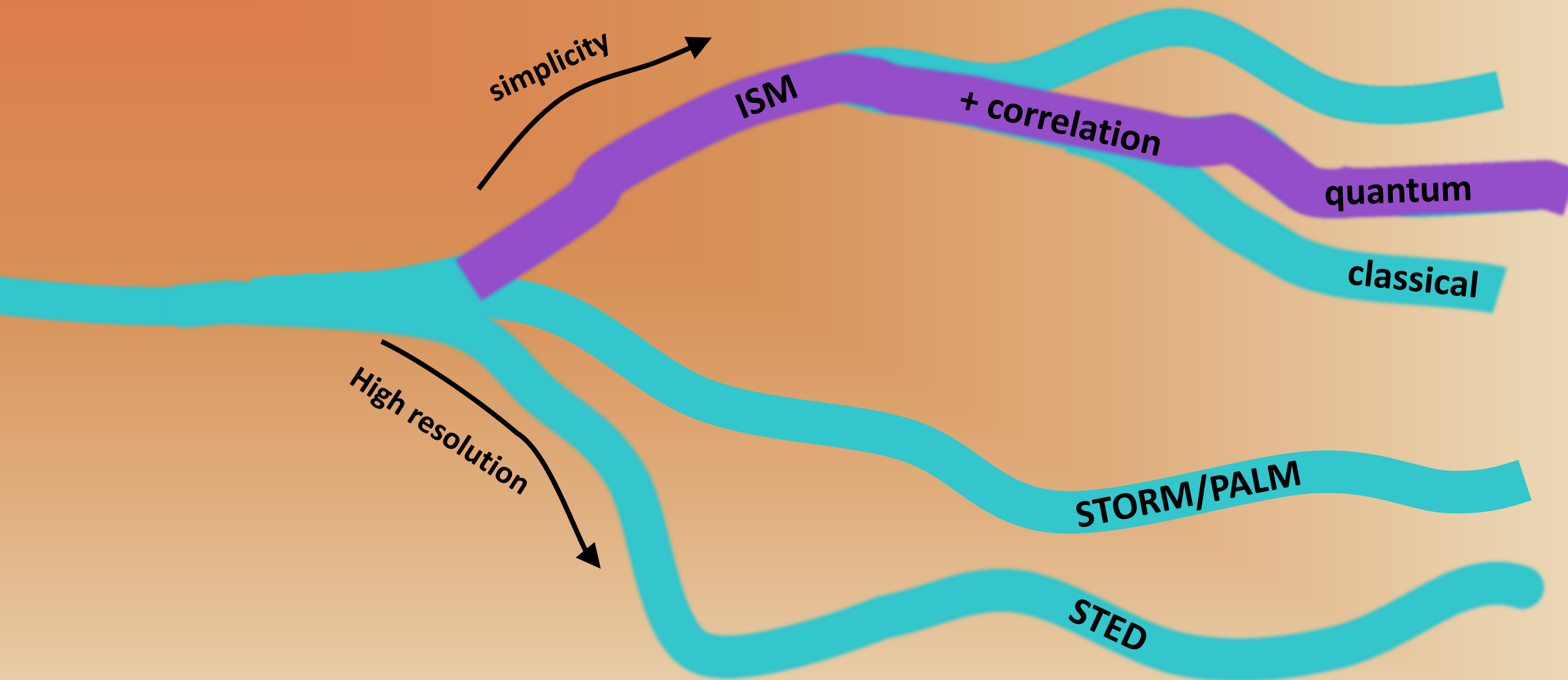
Single photon emitters



$$g^{(2)}(\tau) < 1$$

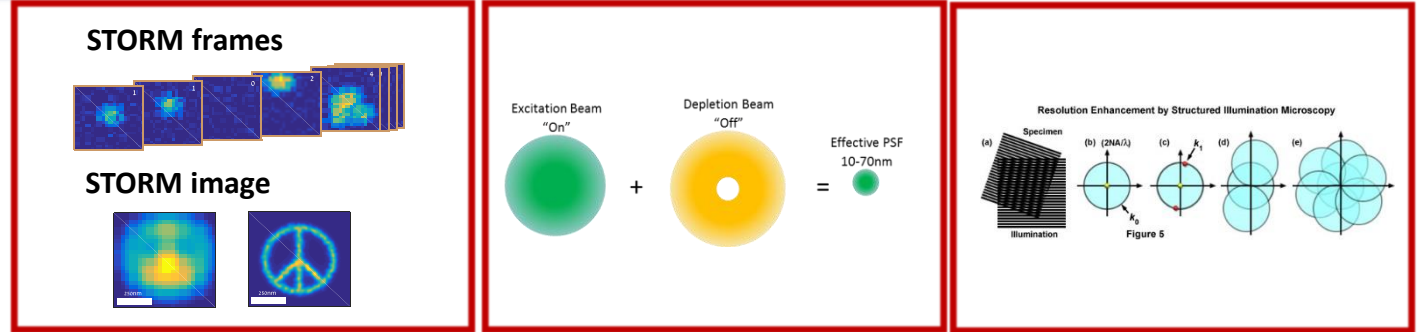
A strictly quantum phenomenon

Super-resolution "flow chart"





Breaking the limit – Super-resolution at a glance



Assumptions:

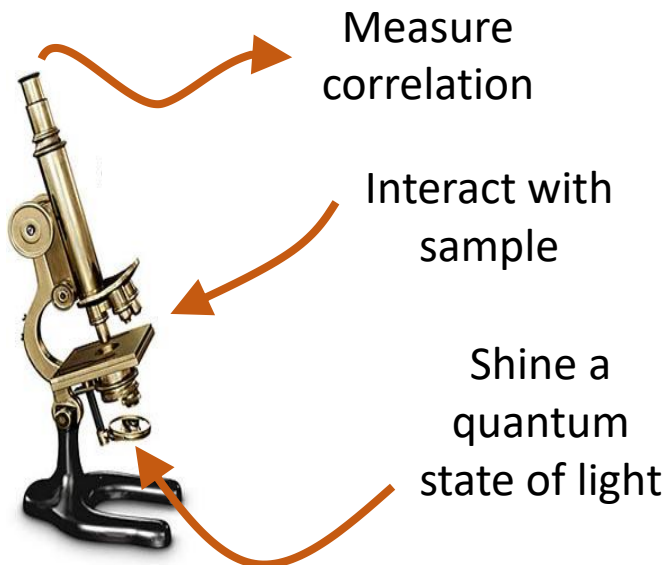
- Linear response
- Uniform illumination
- Far-field detection
- Time independent image
- Classical light

	PALM\STORM	STED	SIM\ISM
• Linear response	✓✗	✗	✓
• Uniform illumination	✓	✗	✗
• Far-field detection	✓	✓	✓
• Time independent image	✗	✓	✓
• Classical light	✓	✓	✓

Can quantum optics contribute?



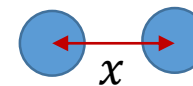
The promise of quantum optics for microscopy



- Phase sensitivity
- Absorption sensitivity
- Quantum lithography

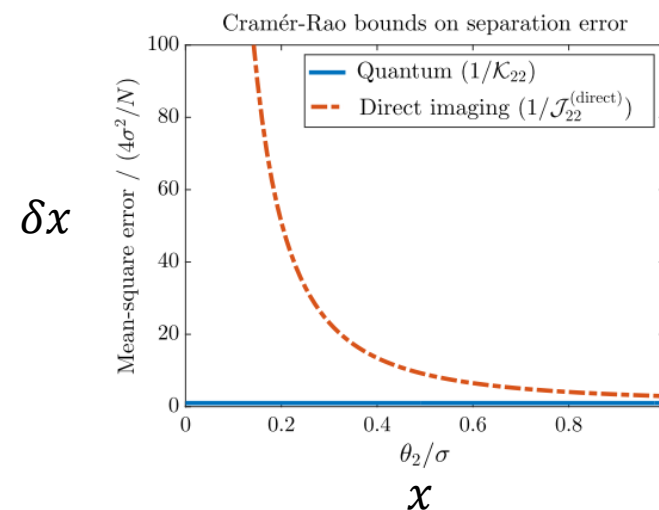
Boto,...,Dowling, *PRL* **85** (2000)
Brida,..., Berchera, *Nat. Photonics*, **4** (2010)
Ono,...,Takeuchi, *Nat. Comm.* **4** (2013)
Israel,...,Silberberg, *PRL* **112** (2014)
Toninelli,...,Padgett, *Optica* **6** (2019)

What is the minimal δx (CRLB)?



Classical: 'Explodes' for low x

Quantum: Constant shot noise



Tsang et al, *PRX* **6** (2016)
Demkowicz-Dobrzański, *PRL* **121** (2018)



A ubiquitous quantum state of light



Classical light source

Quantum emitter

Dye molecules

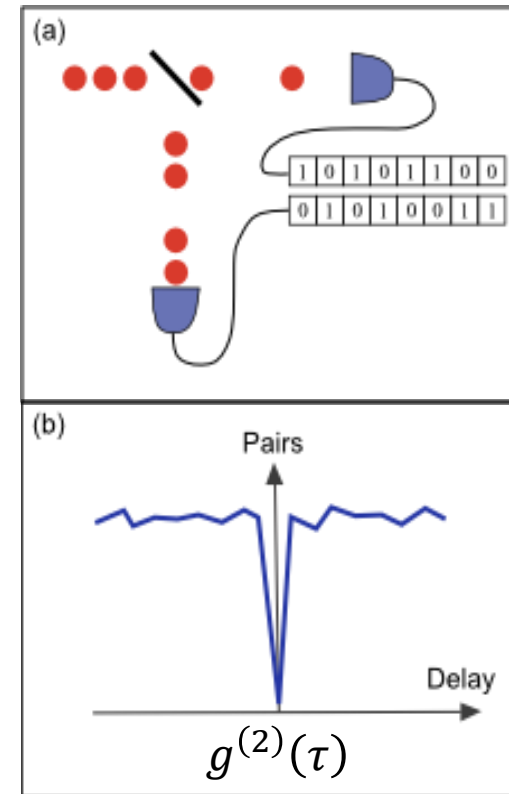
Quantum dots

Solid state defects

Atoms

Some proteins

Single photon at a time

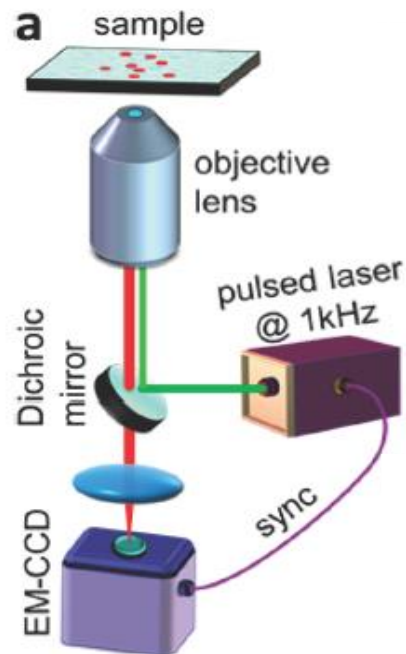


Antibunching

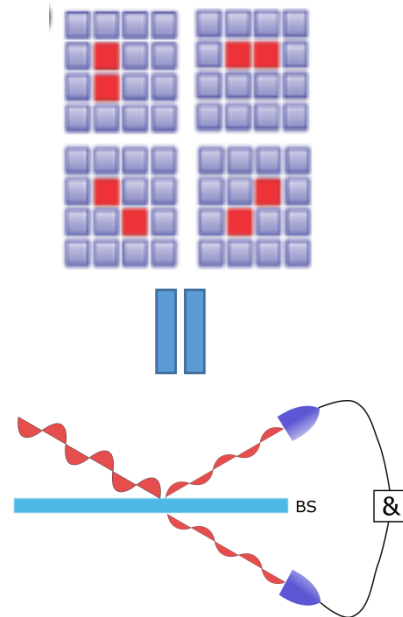


Quantum correlations measured with a camera

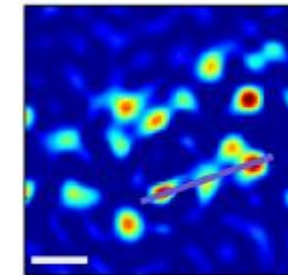
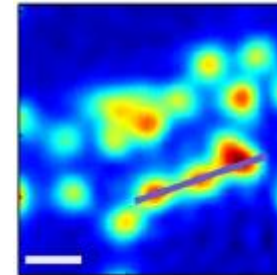
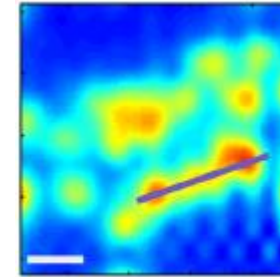
Measure single photons with a camera



Correlate neighboring pixels

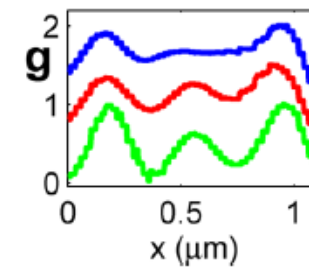


1st order



2nd order

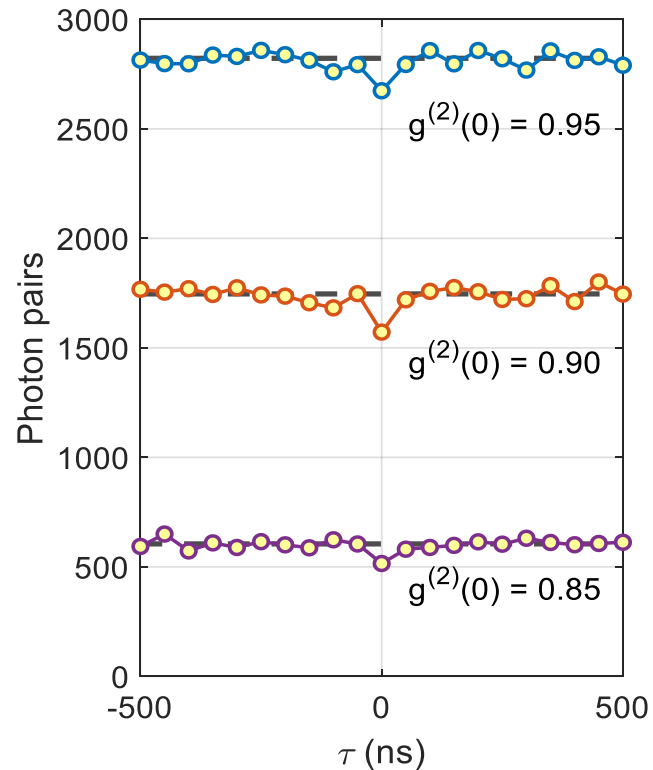
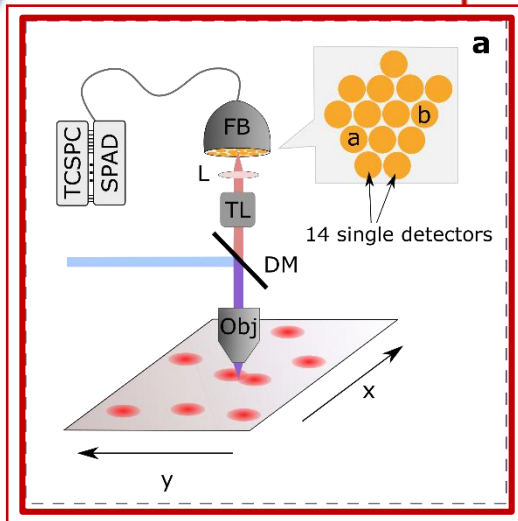
3rd order



Q-ISM: 4 times resolution enhancement

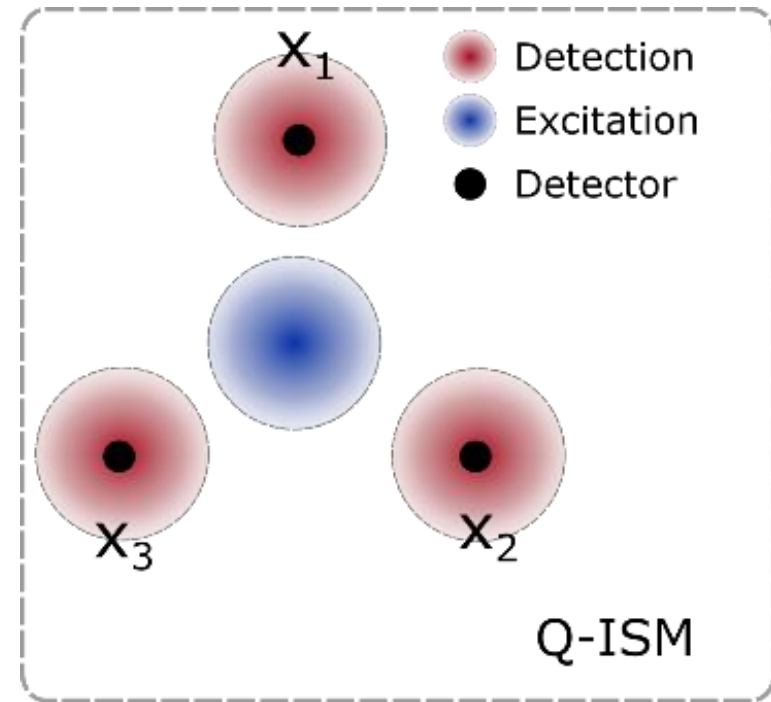


Each emitter is a source of 'missing' photon pairs



$$P_{G2} = (P_{excitation})^2 \cdot P_{det}(x_1) \cdot P_{det}(x_2)$$

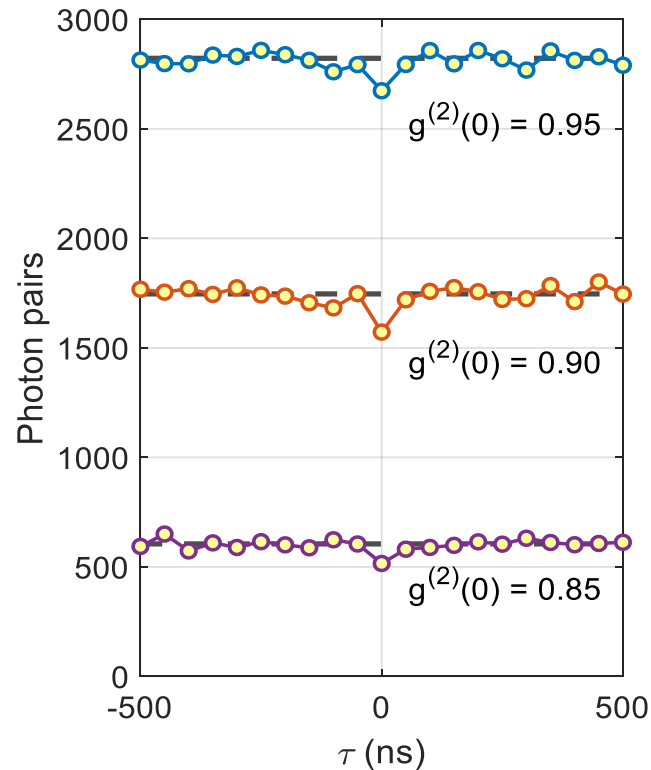
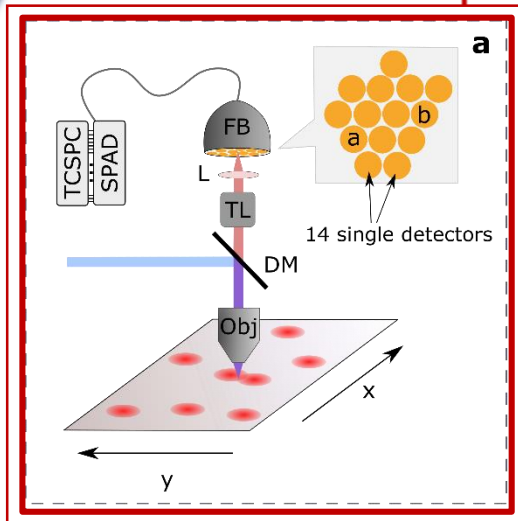
4X resolution enhancement



Q-ISM: 4 times resolution enhancement

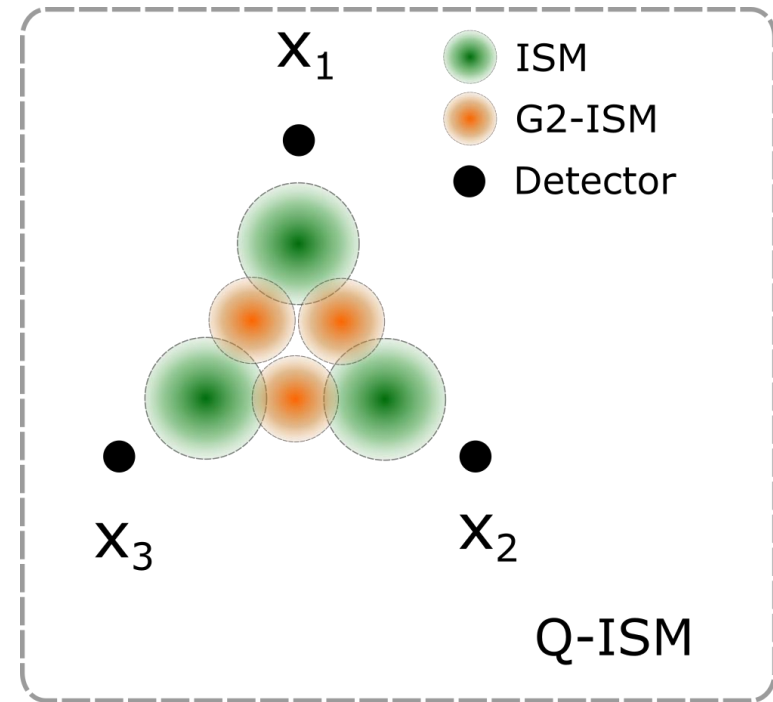


Each emitter is a source of 'missing' photon pairs



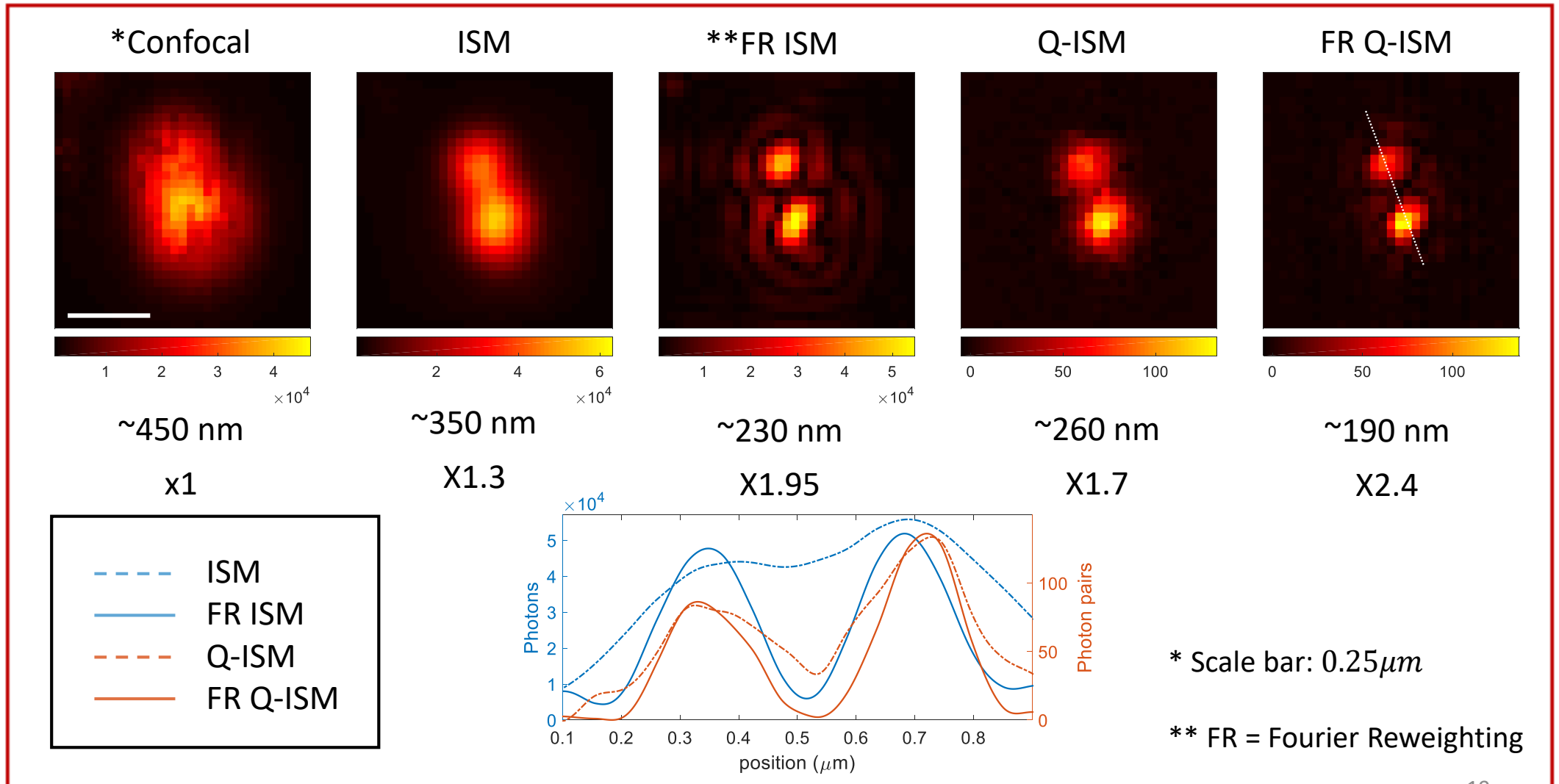
$$P_{G2} = (P_{excitation})^2 \cdot P_{det}(x_1) \cdot P_{det}(x_2)$$

4X resolution enhancement





Q-ISM: Transverse (xy) resolution demonstration



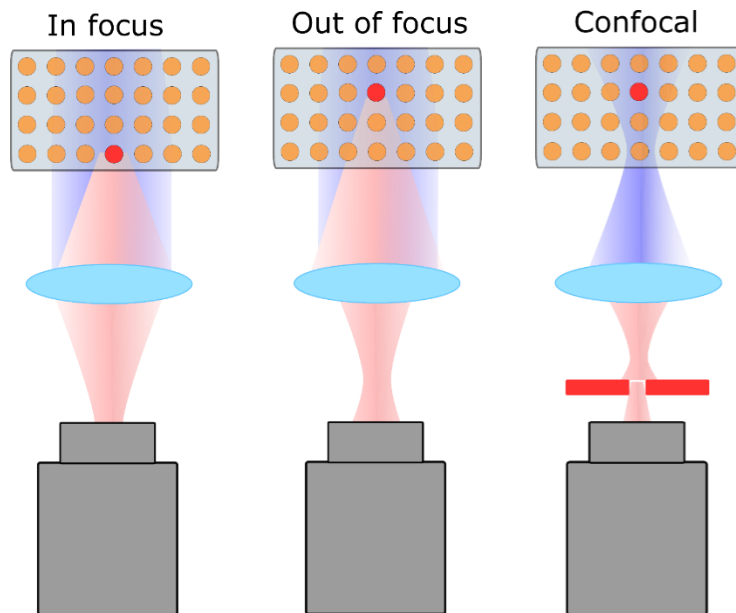
Q-ISM: Axial (z) resolution demonstration

Widefield

In focus and out of focus planes contribute equally

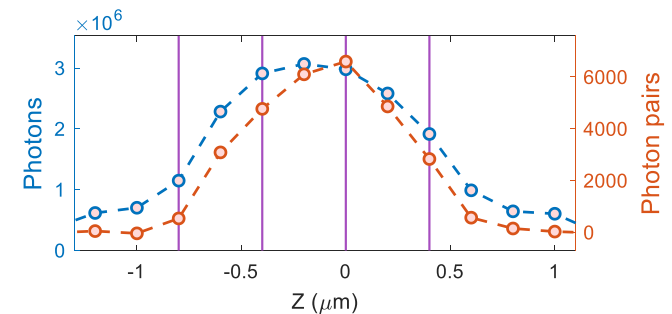
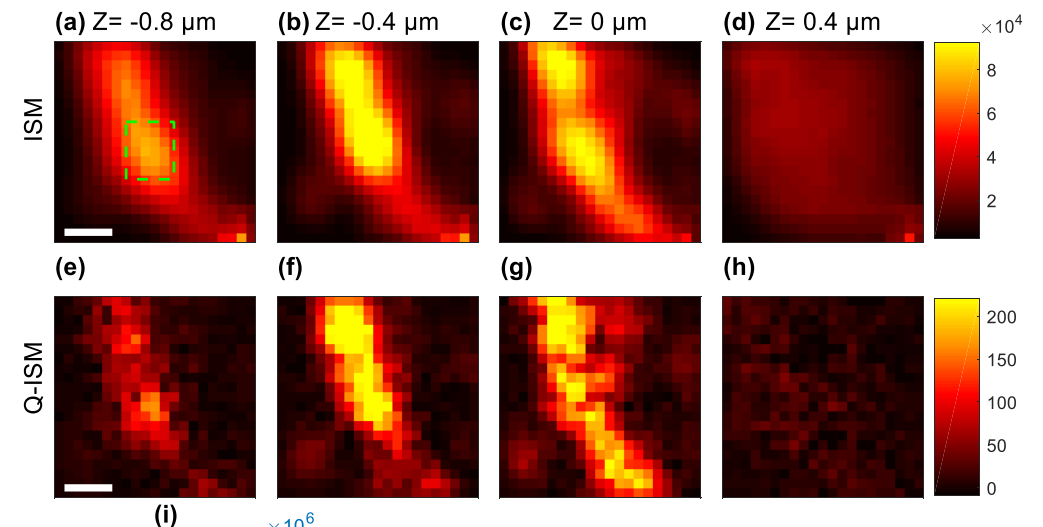
Confocal

$$P_{\text{signal}} = P_{\text{excitation}} \cdot P_{\text{detection}} \propto \frac{1}{z^2}$$



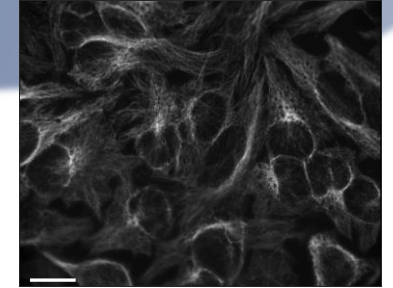
Q-ISM

$$P_{G2} = (P_{\text{excitation}})^2 \cdot P_{\text{det}}(x_1) \cdot P_{\text{det}}(x_2) \propto \frac{1}{z^6}$$



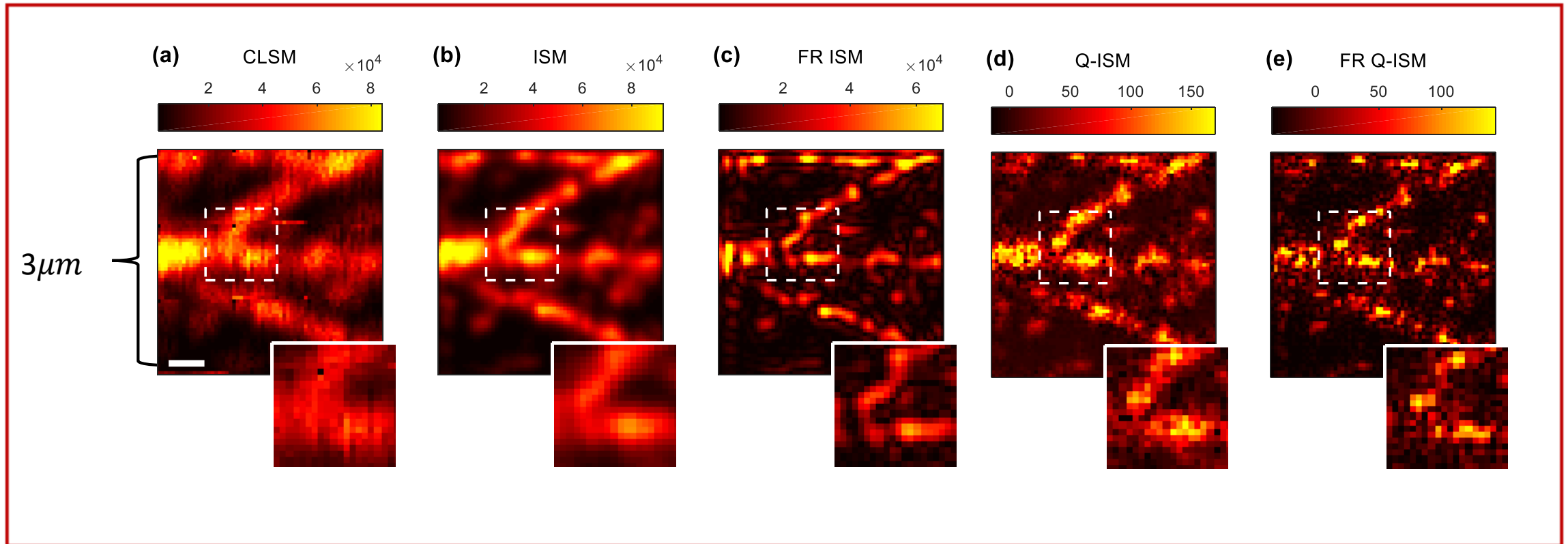


A quantum effect in a biological sample



Widefield fluorescence imaging

3T3 cells. Micro-tubules labeled with quantum dots

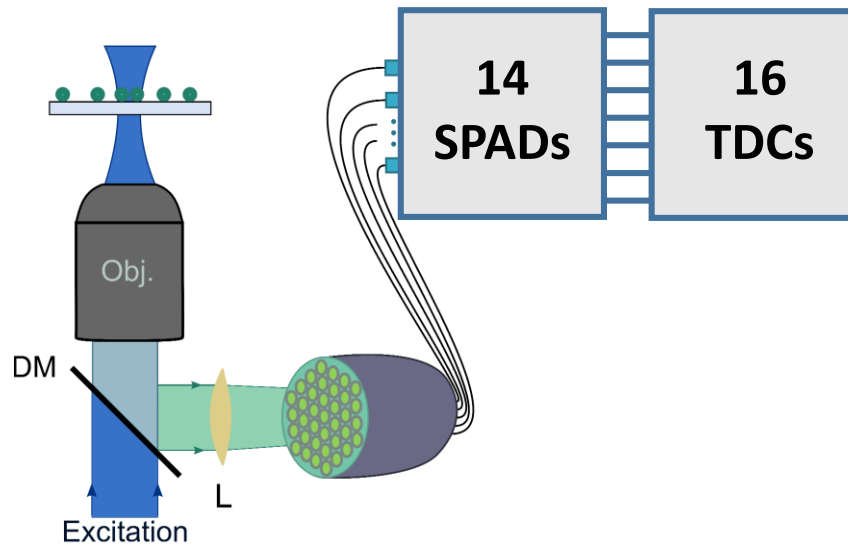


Samples courtesy of Prof. Yuval Ebenstein, TAU

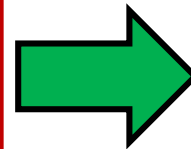


From expensive and cumbersome to SPAD arrays

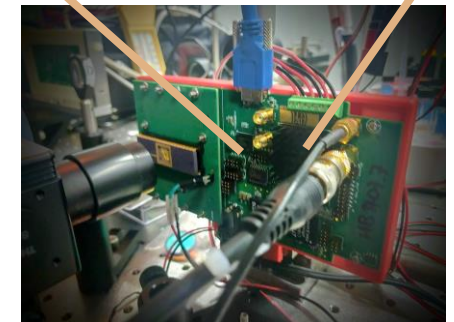
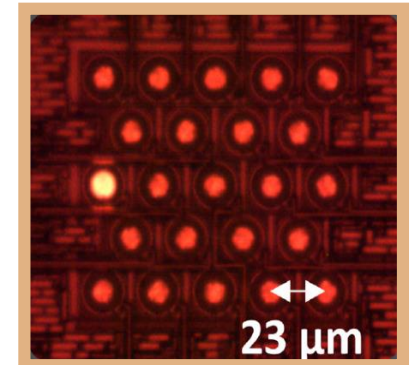
- Image on fiber bundle
- Individual SPADs
- A separate TDC card



Israel, RT *et al.*, *Nat. Comm.*, **8**, (2017)



- SPAD 23
- ~50% max PDP
- FPGA time-stamping

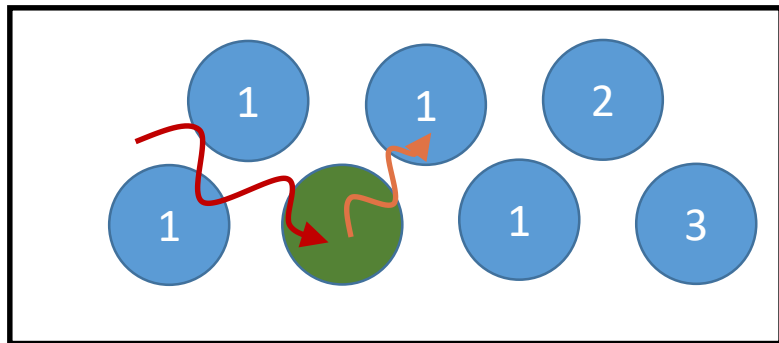


EPFL, AQUA lab



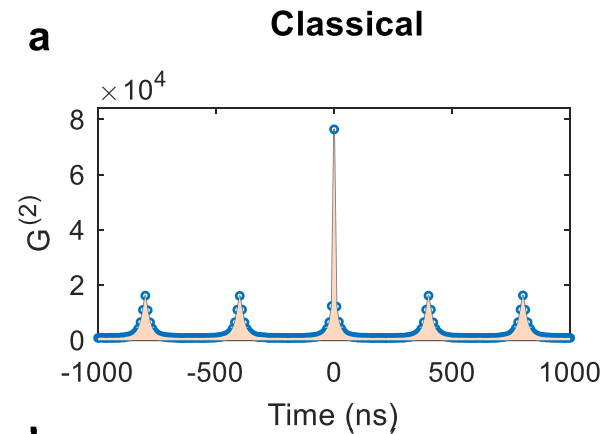
Bruschini *et al.*, *Light: Science & Applications* **8**, 87 (2019)
Antolovic *et al.*, *Opt. Exp.*, **26**, 17 (2018)

HBT with an on-chip SPAD array

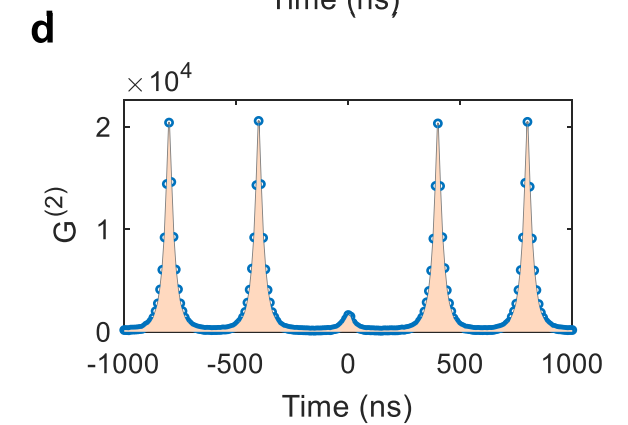
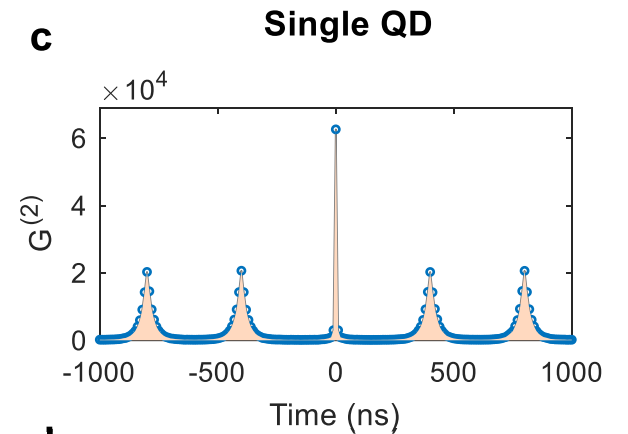
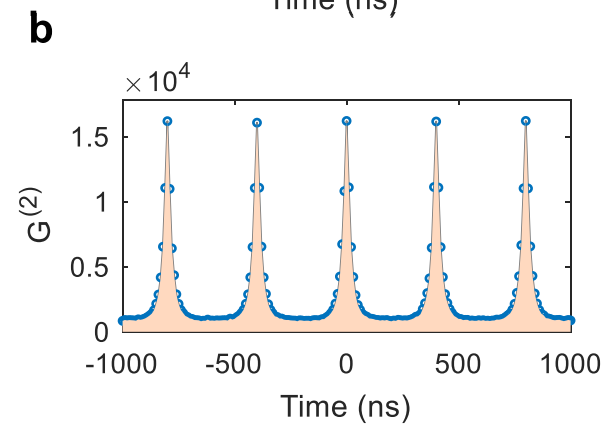


False positive
zero delay pair

No correction

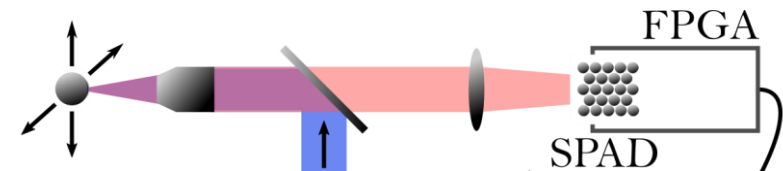
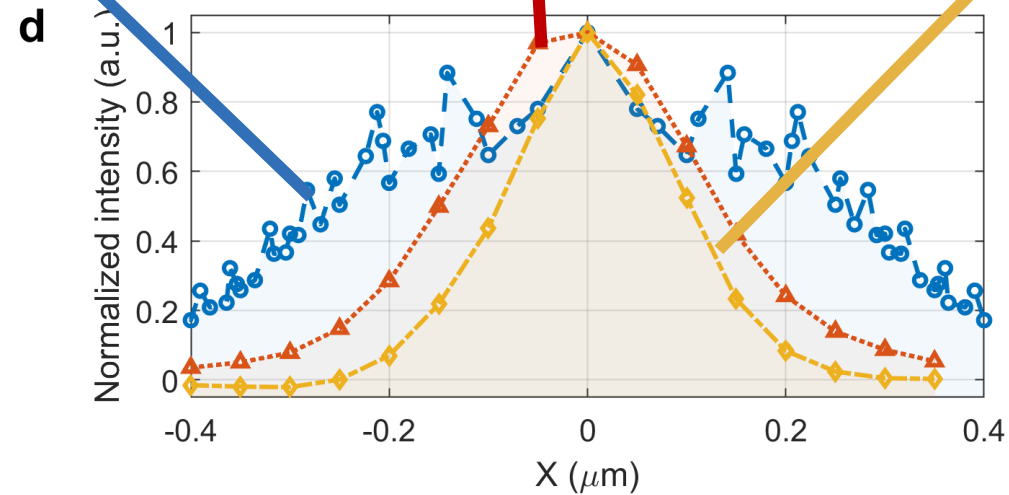
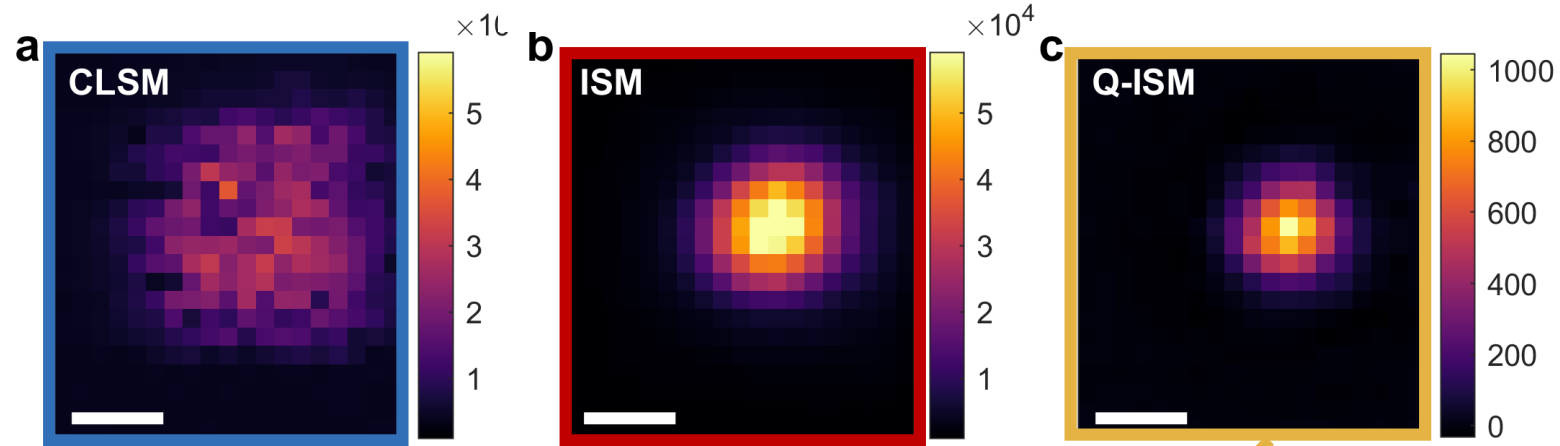


Corrected CT





Q-ISM with a SPAD array



Can we join forces? Sparsity reconstruction



Image similarity sparsity

$$\min_x \{ \|Ax - y\|_2^2 - \lambda \|x\|_1 \}$$

x

A – dictionary (conv with PSF)

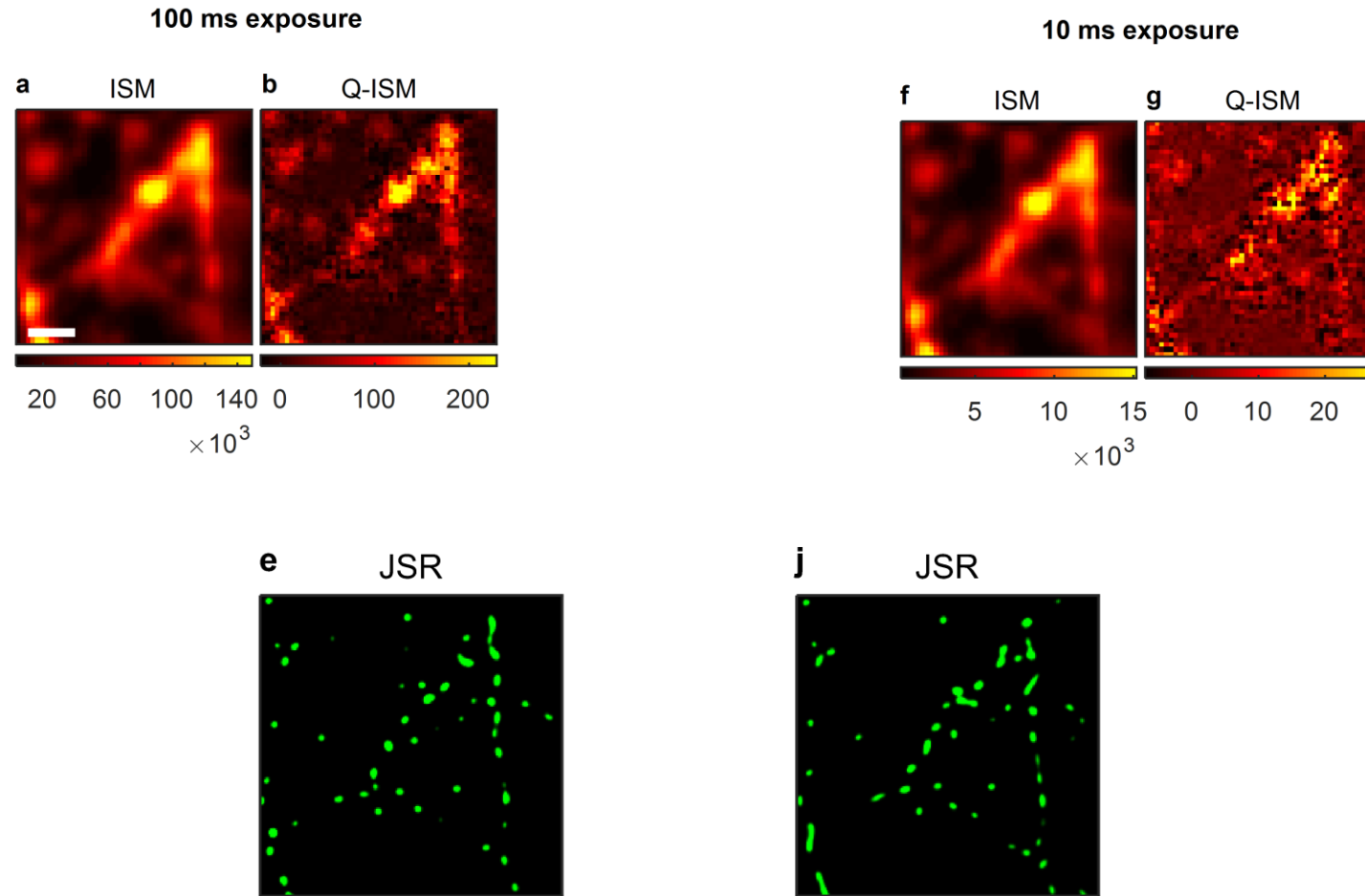
$$\min_{x_1, x_2} \{ \|A_1 x_1 - y_1\|_2^2 + \eta \|A_2 x_2 - y_2\|_2^2 + \lambda \|X\|_{2,1} \}$$

ISM SR ISM JSR

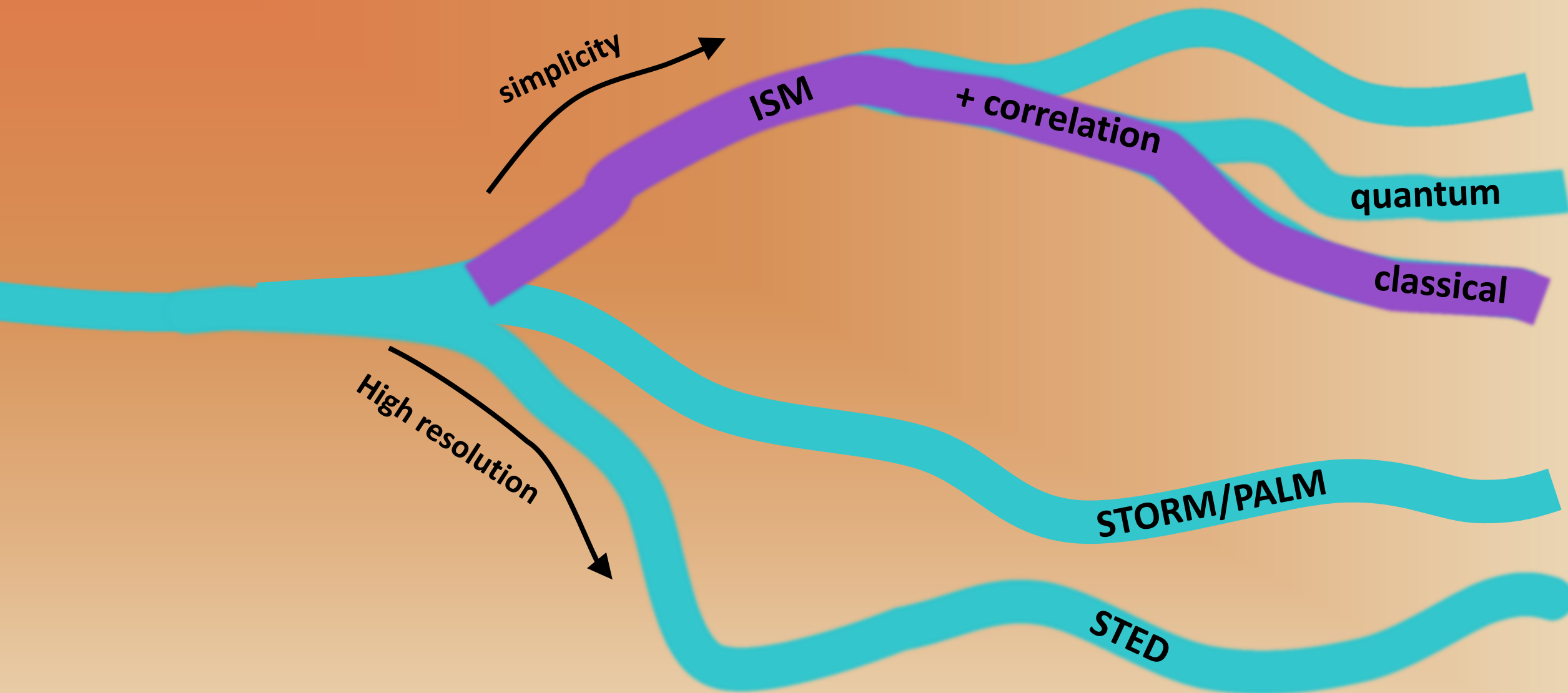
Q-ISM SR Q-ISM



Reconstruction of a cell sample

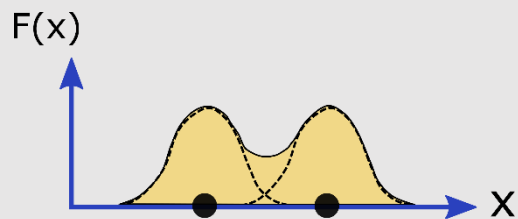


Super-resolution "flow chart"



SOFI: Using emitter fluctuations

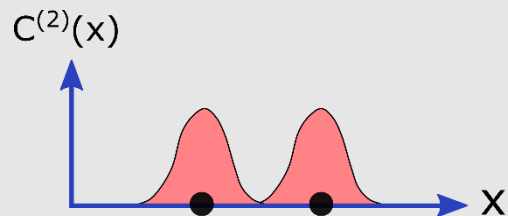
PL image



$$F(x) = F(x+x_0) + F(x-x_0)$$

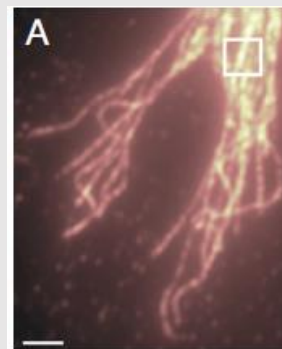
SOFI image

$$C^{(2)}(x) = \langle (F(x, t) - \langle F(x) \rangle)^2 \rangle$$

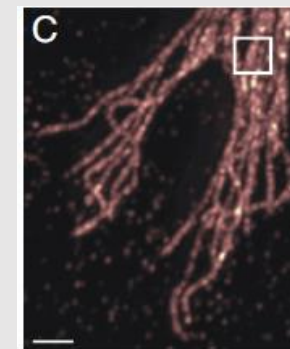


$$C^{(2)}(x) = F(x+x_0)^2 + F(x-x_0)^2$$

Dettinger, ..., Weiss, Enderlein,
PNAS, 106, 52 (2009)



PL image



SOFI image

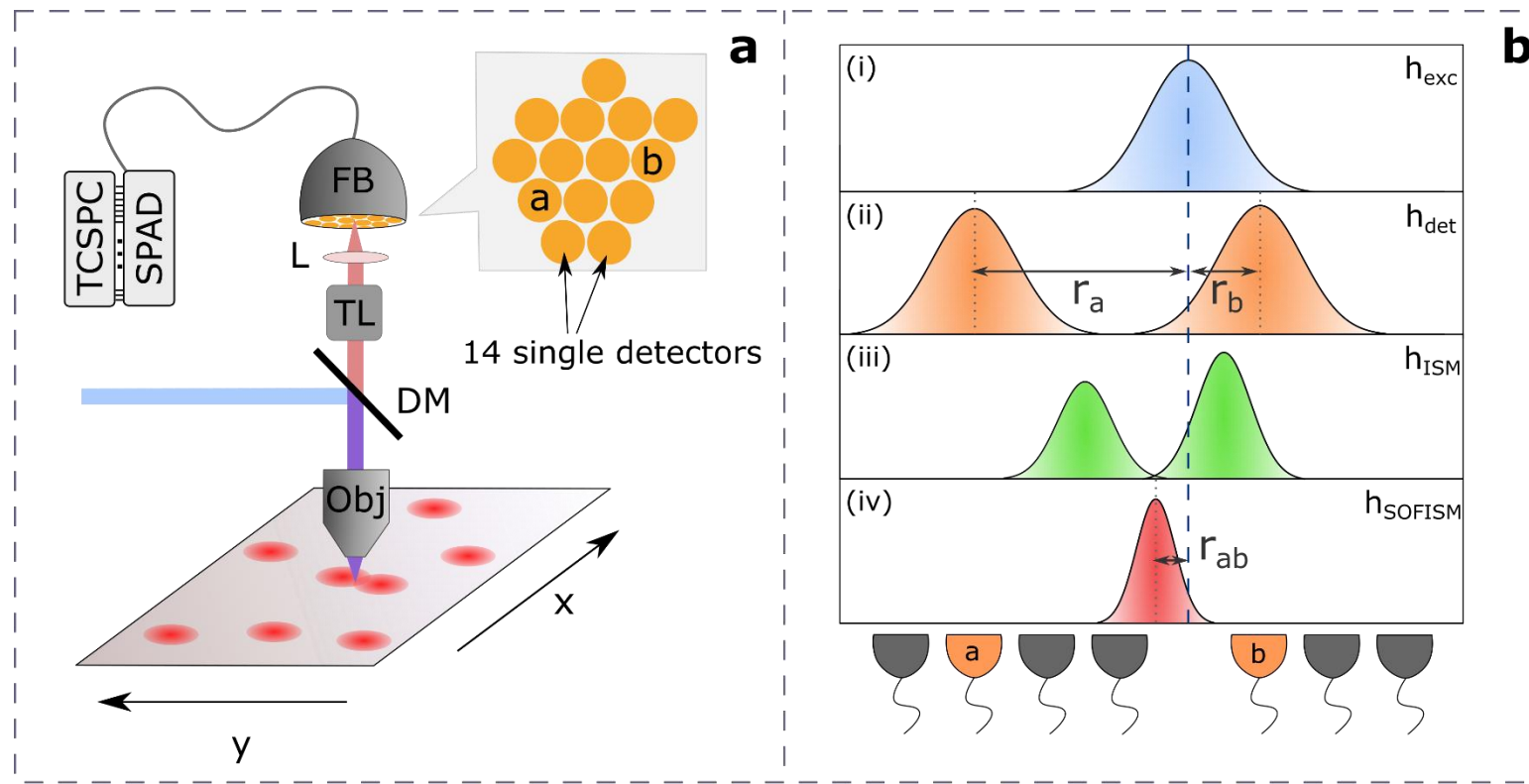
Not only with quantum dots

- **Dyes**
(Dettinger *et al*, Ang. Chem., 49 (2010))
- **Fluorescent proteins**
(Dedecker *et al*, PNAS, 109, (2012))

SOFI + ISM = SOFISM

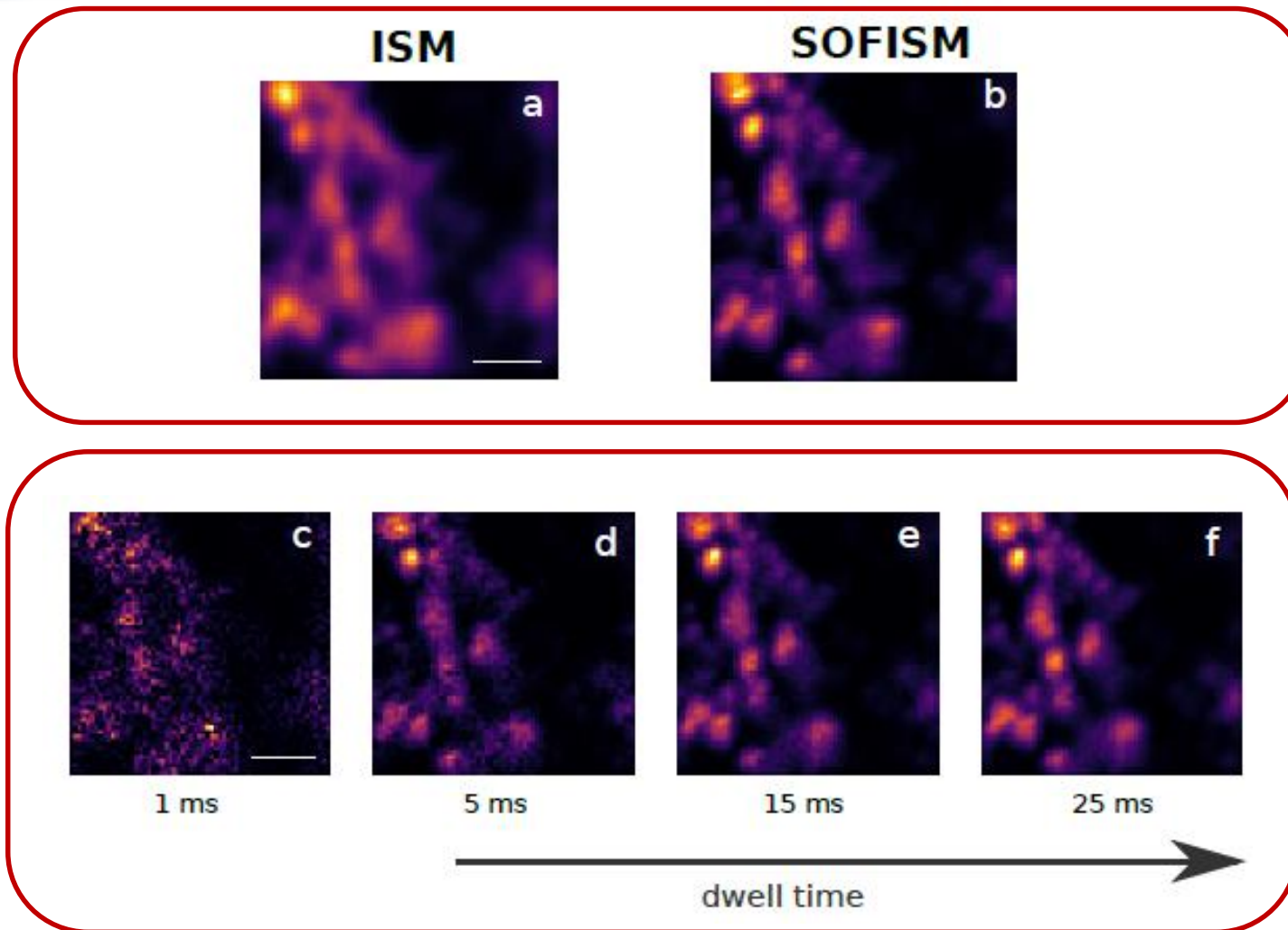
$$C^{(2)}(x) = \langle F_a(x, t) \cdot F_b(x, t) \rangle - \langle F_a(x, t) \rangle \langle F_b(x, t) \rangle$$

$$P_{G2} = (P_{excitation})^2 \cdot P_{det}(x_1) \cdot P_{det}(x_2)$$

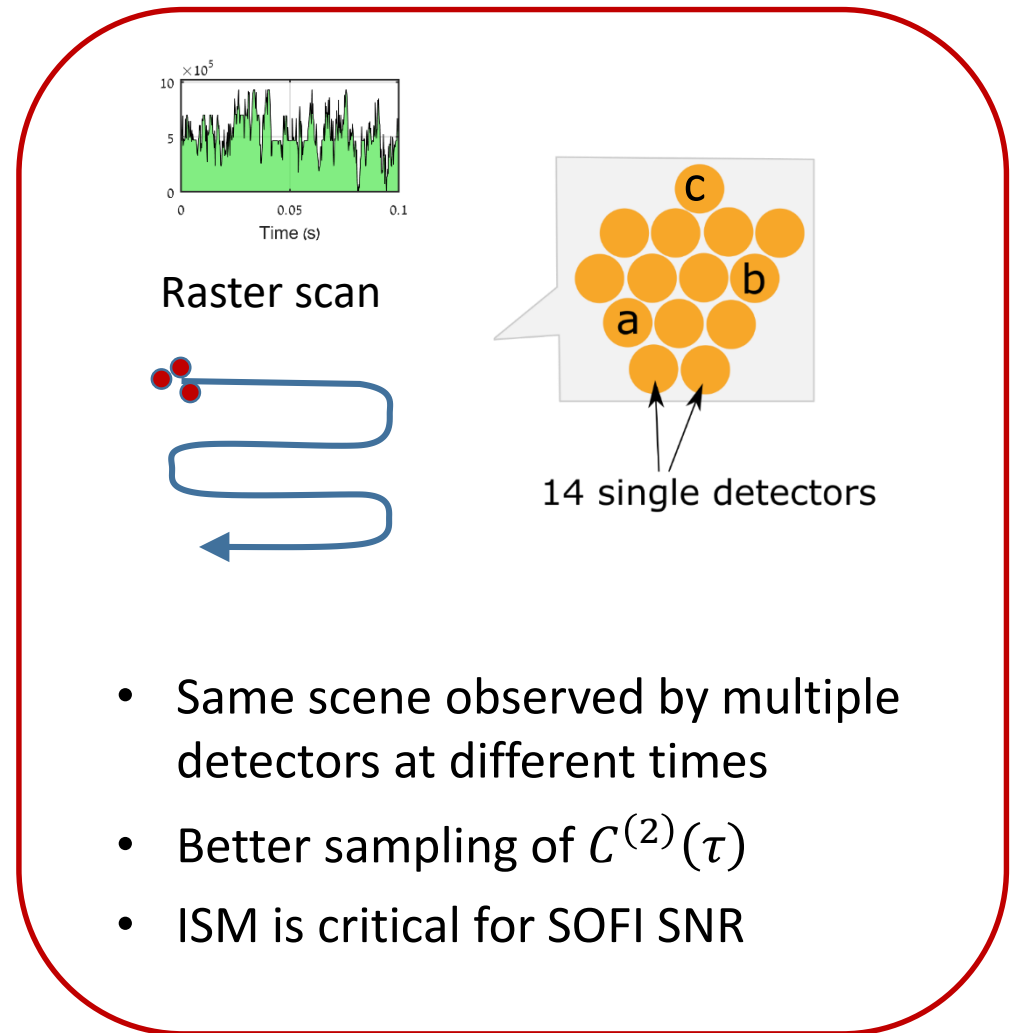
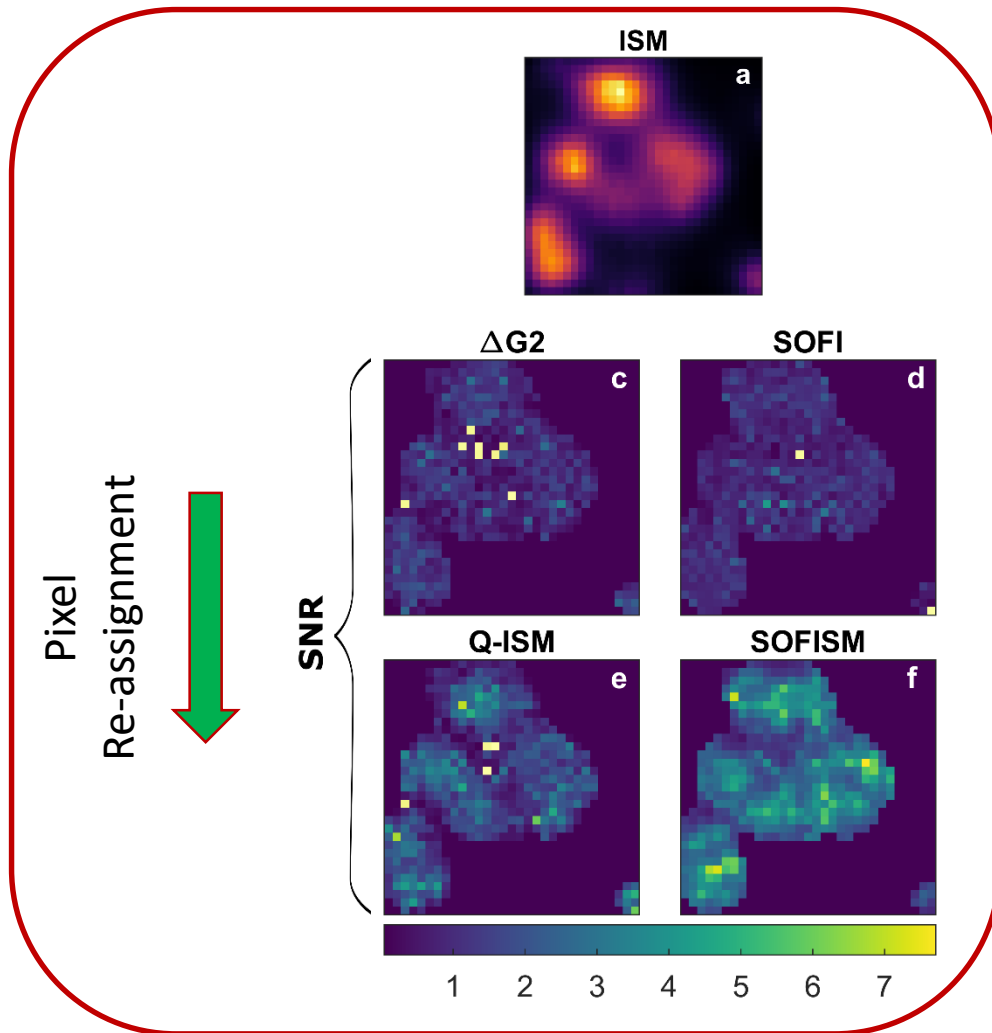




Same resolution shorter acquisition



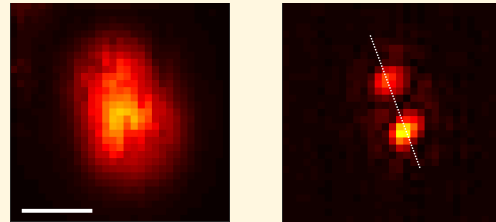
Multiple detectors, multiple sampling periods





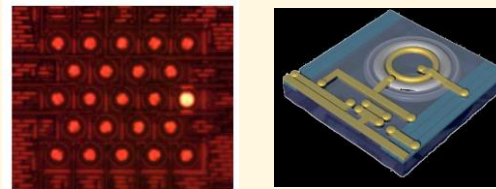
Summary

Image scanning microscopy



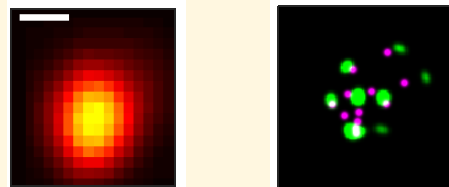
Photon correlation contrast in an image scanning microscopy scheme

Photon correlation with a SPAD array



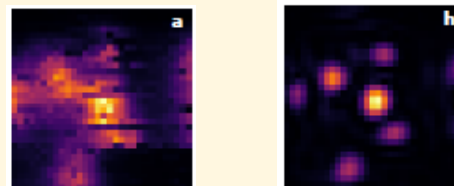
Measure photon correlation with a CMOS SPAD array

Joint sparsity reconstruction



Algorithmic reconstruction from millisecond exposure, quantum and classical data

SOFI and ISM: coming together



Using classical fluctuations as the contrast of image scanning microscopy



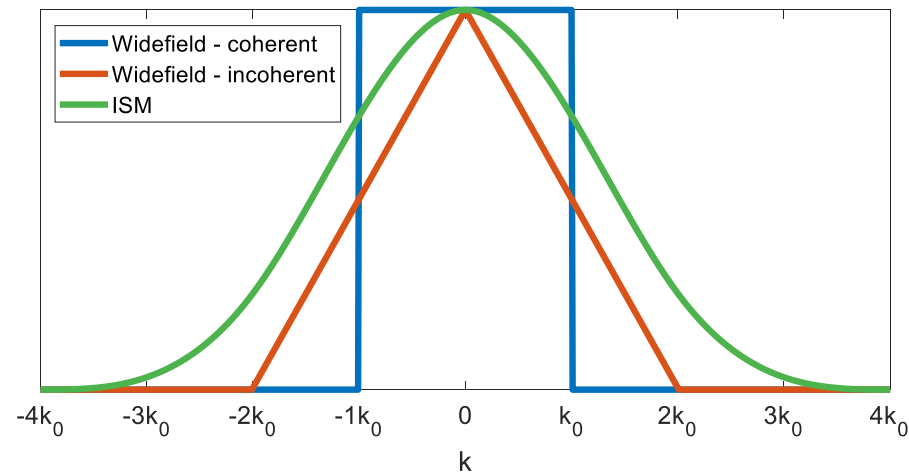
Fourier re-weighting (deconvolution)

The point spread function (PSF) of ISM

Real space $h_{ISM}(x) = P_{excitation} \cdot P_{detection} = h_{in}(x) \cdot h_{in}(x) = h_{in}^2(x)$

Momentum space $\tilde{h}_{ISM}(k) = h_{in}(k) * h_{in}(k)$

1D PSF in
momentum space



Counting the missing photon pairs

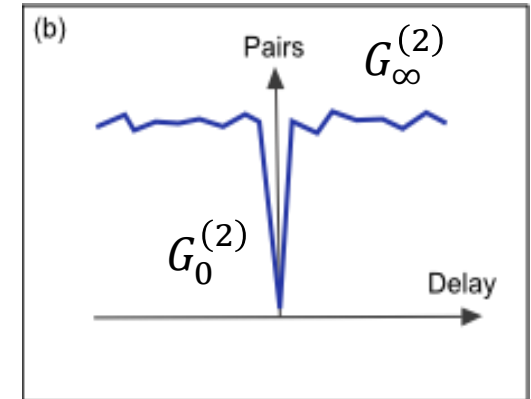
G2ISM

$$G_{AB}^{(2)}(x) = G_{\infty}^{(2)}(x) - G_0^{(2)}(x) = \sum_{i=1}^n [h_e(x_i - x_s)]^2 \cdot [h_{im}(x_i - x_s)]^2$$

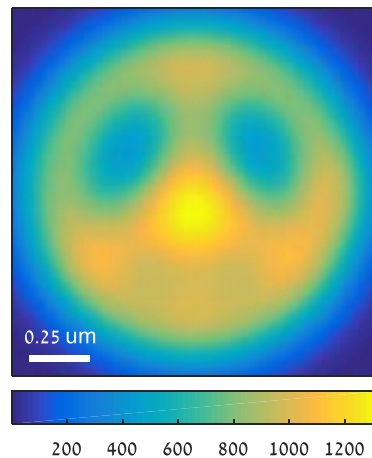
Simulated

66 QDs. 25nm, 250msec steps.

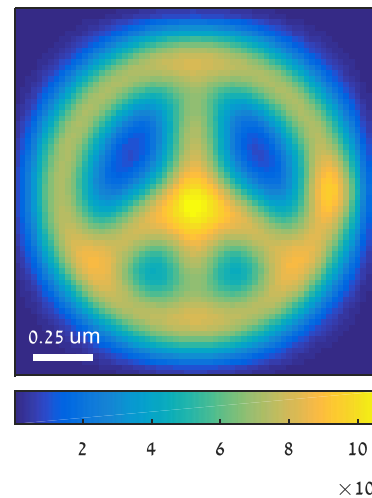
Including dark current and Poissonian noise



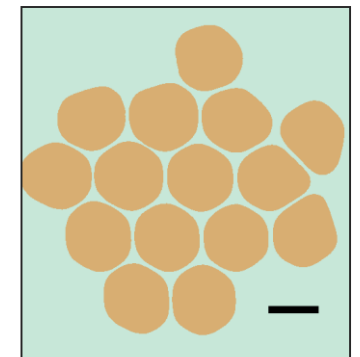
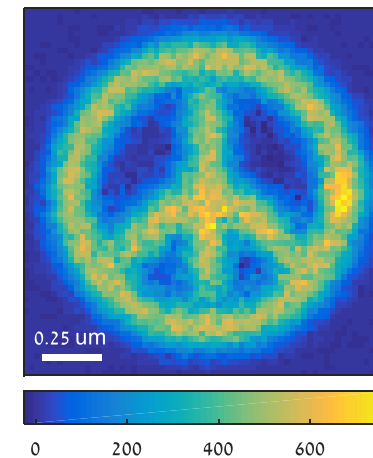
Widefield



ISM

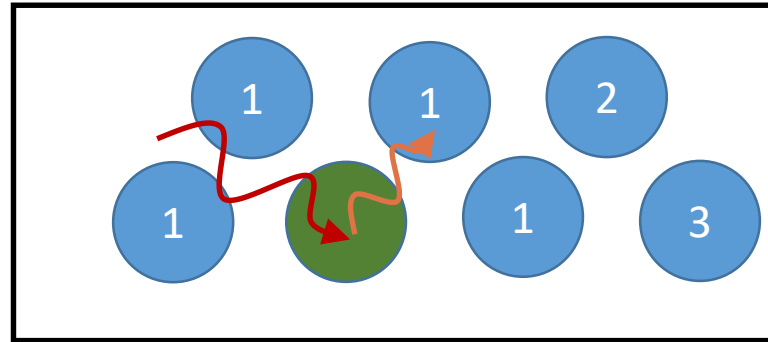


G2ISM



HBT with an on-chip SPAD array

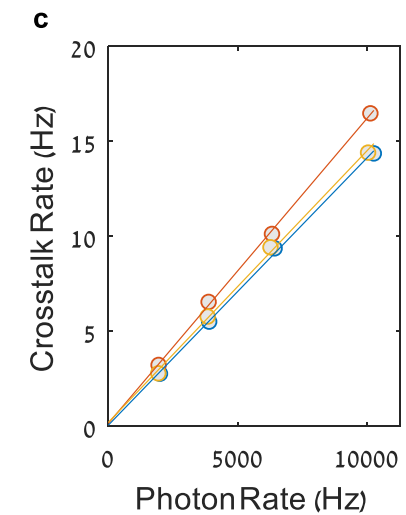
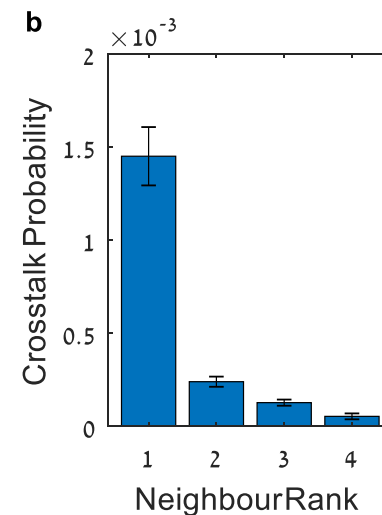
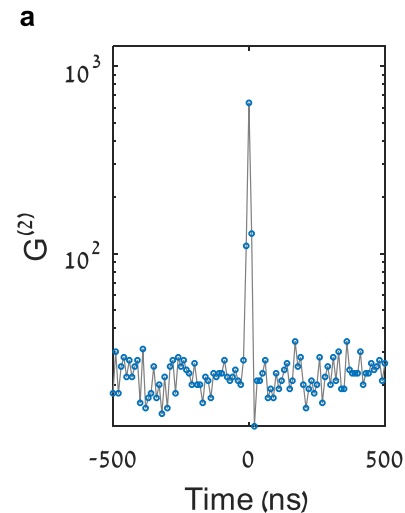
Main challenge:
Optical cross-talk



False positive
zero delay pair

Hesong Xu et al. Procedia Engineering 87 (2014)

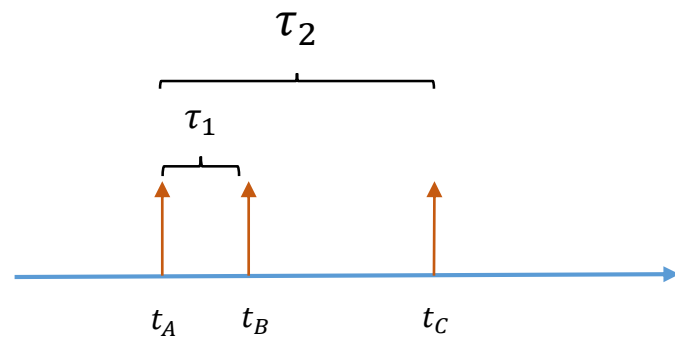
Nearest neighbor
cross-talk
 $\sim 1.5 \cdot 10^{-3}$



Higher order HBT with one port



Three
photon
events



$$\tau_1 = t_B - t_A$$

$$\tau_2 = t_C - t_A$$

